

# Impulsive Stabilization and Application to a Population Growth Model\*

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**Abstract:** This paper studies the problem of impulsive stabilization of a system of autonomous ordinary differential equations. Necessary and sufficient conditions are established for a given state, which need not be an equilibrium point of the system, to be impulsively stabilizable. These results are applied to a three-species population growth model. In the population growth model, it is shown that by impulsively regulating one species, the population of all three species can be maintained at a positive level, which otherwise would drop to a level of extinction for one of the species.

**Keywords:** *Impulsive stabilization; control; population growth model.*

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