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## Variational Analysis and Error Estimate of Contact Problem for Thermo-Viscoelastic Bodies with Long-Term Memory

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**Abstract:** This paper investigates a contact problem involving the quasistatic interaction between two bodies characterized by thermo-viscoelasticity with long-term memory. The mechanical, thermal contact is captured through the sub-differential condition, which represents the frictional interaction. We establish a variational formulation for the model and we prove the existence of a unique weak solution. Subsequently, a numerical investigation is conducted, employing both finite element and finite difference methods. This computational approach allows for the derivation of a discrete approximation of the error associated with the analyzed model.

**Keywords:** fixed point; frictional contact; finite element method; thermopiezoelectric; weak solution.

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