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## First Integral of a Class of Two Dimensional Kolmogorov Systems

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**Abstract:** In this paper, we are interested in studying the existence of a first integral and the curves which are formed by the trajectories of the autonomous planar Kolmogorov systems. Concrete examples exhibiting the applicability of our result are introduced.

**Keywords:** *dynamical system; Kolmogorov system; first integral; periodic orbits; limit cycle.* 

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## 1 Introduction

By definition, an autonomous planar Kolmogorov system is a system of the form

$$\begin{cases} x' = \frac{dx}{dt} = xF(x,y), \\ y' = \frac{dy}{dt} = yG(x,y), \end{cases}$$
(1)

these equations are equivalent to the differential equation

$$\frac{dy}{dx} = \frac{yQ\left(x,y\right)}{xP\left(x,y\right)}$$

where F, G are two functions in the variables x and y and the derivatives are taken with respect to the time variable. The theory of differential equations is one of the basic tools of mathematical science [1–3,20]. System (1) is frequently used to model the iteration of two species occupying the same ecological niche [14, 16]. There are many

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